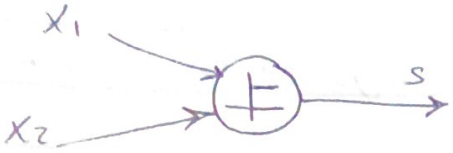
hebbian



* $e = d - s$

for $d=0$ $s=0$ $\Rightarrow$ correct

for $d=0$ $s=1$ $\Rightarrow$ overprediction

for $d=1$ $s=0$ $\Rightarrow$ underprediction

for $d=1$ $s=1$ $\Rightarrow$ correct

S1

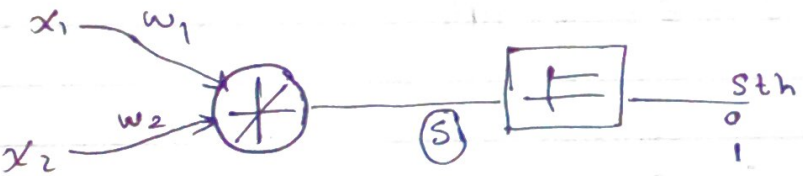
$w' = [w'_1 \quad w'_2]$

S2

$w'_1 = w^o_1 + \Delta w$

$\Delta w = e * X * B$

New Learning method: Linear neuron



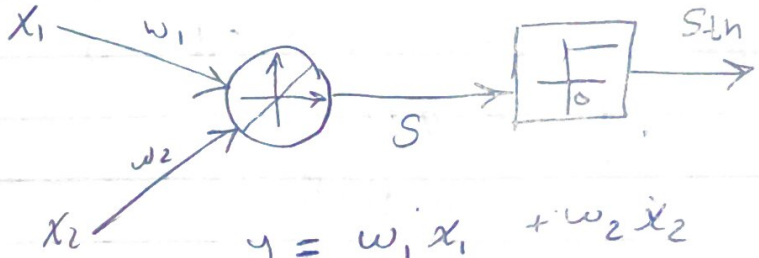
لغرض $\rightarrow$ $S = y$; $e = d - s$

assume $S = -1.1 < 0 \Rightarrow Sth = 0$ $d=1$ (underpred.)

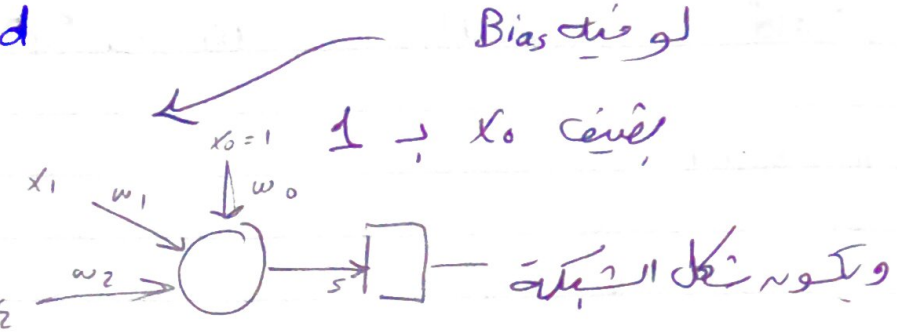
$S = 2 > 0$ $Sth = 1$ $d=1$ (correct)

* example

x_1	x_2	d
0.3	0.7	1
-0.6	0.3	0
-0.1	-0.8	0
0.1	-0.45	1



x_0	x_1	x_2	d
⋮	⋮	⋮	⋮



<< Bias مهم جدا جدا >>

* initial weight Assume $\beta = 0.5$

$w_1^\circ = 0.8$ $w_2^\circ = -0.5$.

(Training iteration 1)

* Sample 1 (0.3, 0.7) ; d = 1

$y = (0.8)(0.3) + (0.7)(-0.5) = -0.11$

$S = y = -0.11 < 0$

$\Rightarrow sth = 0$; d = 1 (under prediction)

$e = d - S = 1 + 0.11 = 1.11$

update weights

$\therefore w_1' = w_1^\circ + \beta x_1 e = 0.9665$

$w_2' = w_2^\circ + \beta x_2 e = -0.1115$

* Sample 1 with w'

$y = 0.2119 = S > 0 \Rightarrow sth = 1$ & $d = 1$ (correct)

* sample 2 (-0.6 , 0.3) (d=0)

$w_1' = 0.9665$

$w_2' = -0.1115$

$y = -0.613 = S < 0 \Rightarrow sth = 0$; d = 0 (correct)

* Sample 3 (-0.1 , 0.8) (d=0)

$w_1' = 0.9665$

$w_2' = -0.1115$

$y = -0.00745 = S < 0 \Rightarrow sth = 0$; d=0. (correct)

* sample 4 $(0.1, -0.45)\ (d=1)$

$w_1' = 0.9665$

$w_2' = -0.1115$

$y = 0.1468 = S > 0 \Rightarrow S_{th} = 1 \ \& \ d = 1$ (correct)

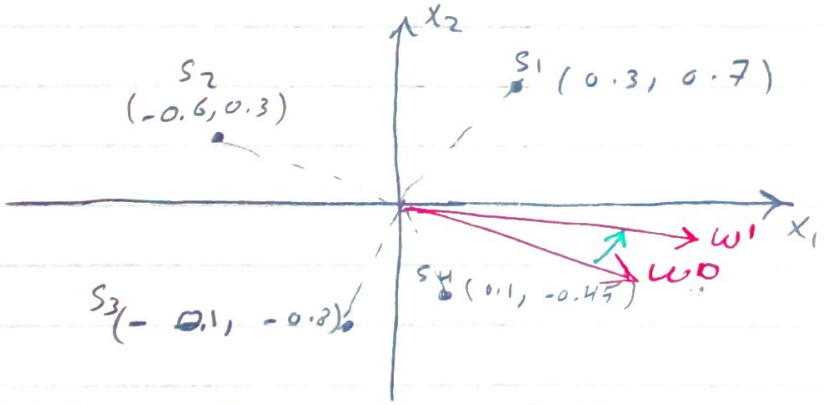
final weight $w' = [0.9665 \quad -0.1115]$ ← vector

Testing

x_1	x_2	$y = S$	S_{th}	d	classification
0.3	0.7	0.2119	1	1	Correct
-0.6	0.3	-0.613	0	0	//
-0.1	-0.8	-0.00745	0	0	//
0.1	-0.45	0.1468	1	1	//

Motion of weight vectors during Learning

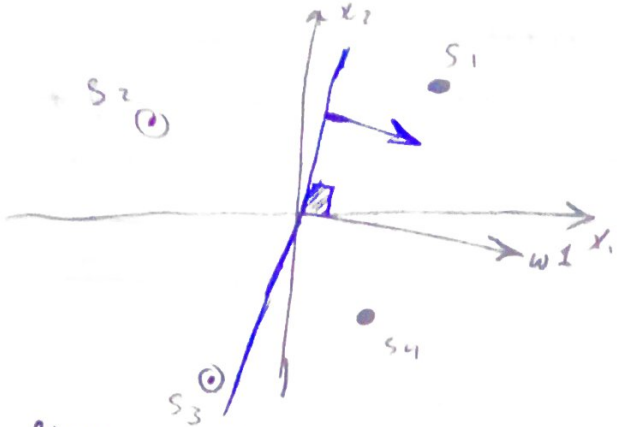
$$w^0 = \begin{bmatrix} 0.8 \\ -0.5 \end{bmatrix}, \quad w^1 = \begin{bmatrix} 0.9665 \\ -0.1115 \end{bmatrix}$$



* حصل underprediction وأنا بحاول مع S_1، فمضطر أحرك w في اتجاه S_1

* لازم نحط الفعل (مطلوب) (باللون الأزرق)

Classification Boundary



seperation line $y = 0$.

$0.9665\, x_1 - 0.1115\, x_2 = 0$

$\Rightarrow x_2 = 8.67\, x_1$

لاحظ أن اتجاه ال weight هو اتجاه ال orientation